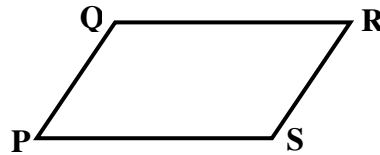


Section 8.2 – Properties of Parallelograms

A _____ is a quadrilateral with both pairs of opposite sides parallel.

The symbol used for a parallelogram is \square . In the diagram for $\square PQRS$, $\overline{PQ} \parallel \overline{RS}$ and $\overline{QR} \parallel \overline{SP}$.

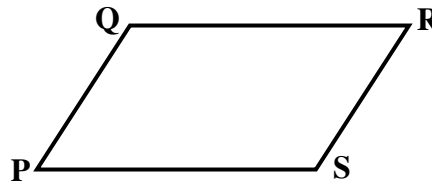


Note: Label Diagram

Properties of a Parallelogram

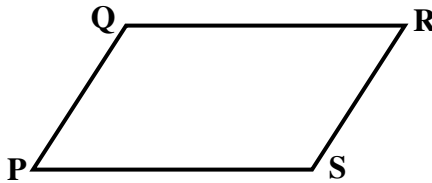
If a quadrilateral is a parallelogram, then its **opposite sides** are congruent.

$$\overline{PQ} \cong \overline{RS} \text{ and } \overline{SP} \cong \overline{QR}$$



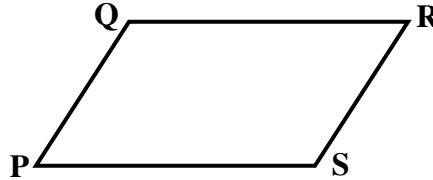
If a quadrilateral is a parallelogram, then its **opposite angles** are congruent.

$$\angle P \cong \angle R \text{ and } \angle Q \cong \angle S$$



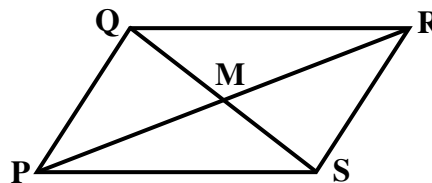
If a quadrilateral is a parallelogram, then its **consecutive angles** are supplementary.

$$m\angle P + m\angle Q = 180^\circ, m\angle Q + m\angle R = 180^\circ, \\ m\angle R + m\angle S = 180^\circ, m\angle S + m\angle P = 180^\circ$$



If a quadrilateral is a parallelogram, then its **diagonals bisect** each other.

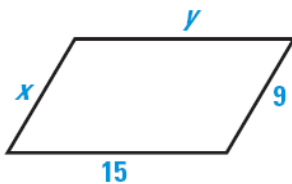
$$\overline{QM} \cong \overline{SM} \text{ and } \overline{PM} \cong \overline{RM}$$



Ex 1:

Find the value of the variable(s) for the parallelogram.

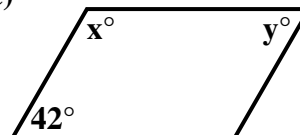
a)



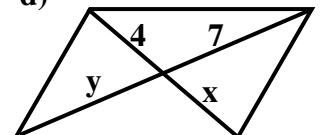
b)



c)



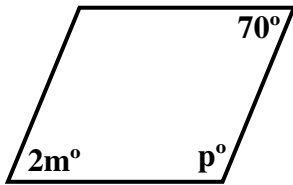
d)



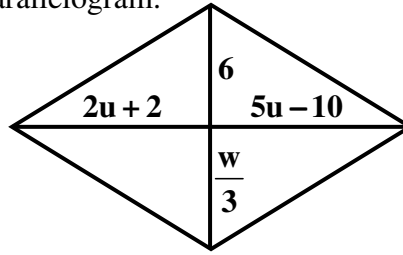
Ex 2:

Find the value of each variable in the parallelogram.

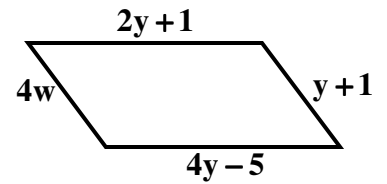
a)



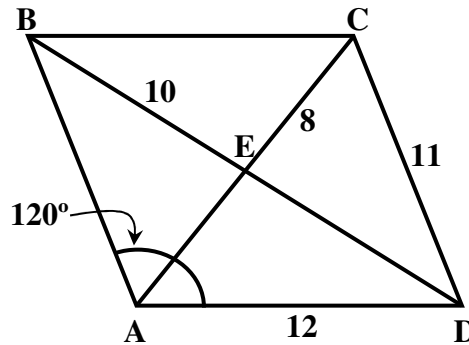
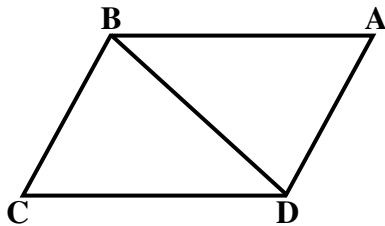
b)



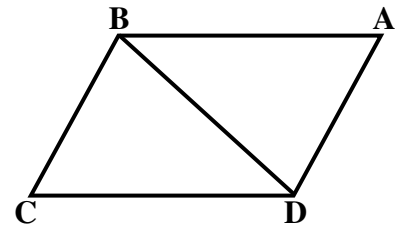
c)

**Ex 3:**

Find the measure in parallelogram ABCD.

a) $DE =$ b) $BC =$ c) $m\angle ABC =$ d) $BA =$ e) $m\angle DCB =$ f) $AC =$ **Ex 4:****Given:** $\square ABCD$ **Prove:** $\triangle ABD \cong \triangle CDB$ **Note:** There are many approaches to solving this proof.**Approach #1**

Statement	Reason
1. $\square ABCD$	1. Given
2. $\overline{BA} \cong \overline{CD}$	2. _____
3. $\angle CDB \cong \angle ABD$	3. _____
4. $\overline{BD} \cong \overline{BD}$	4. _____
5. $\triangle ABD \cong \triangle CDB$	5. _____

Approach #2

Statement	Reason
1. $\square ABCD$	1. Given
2. $\angle C \cong \angle A$	2. _____
3. $\angle CBD \cong \angle ADB$	3. _____
4. $\overline{BD} \cong \overline{BD}$	4. _____
5. $\triangle ABD \cong \triangle CDB$	5. _____