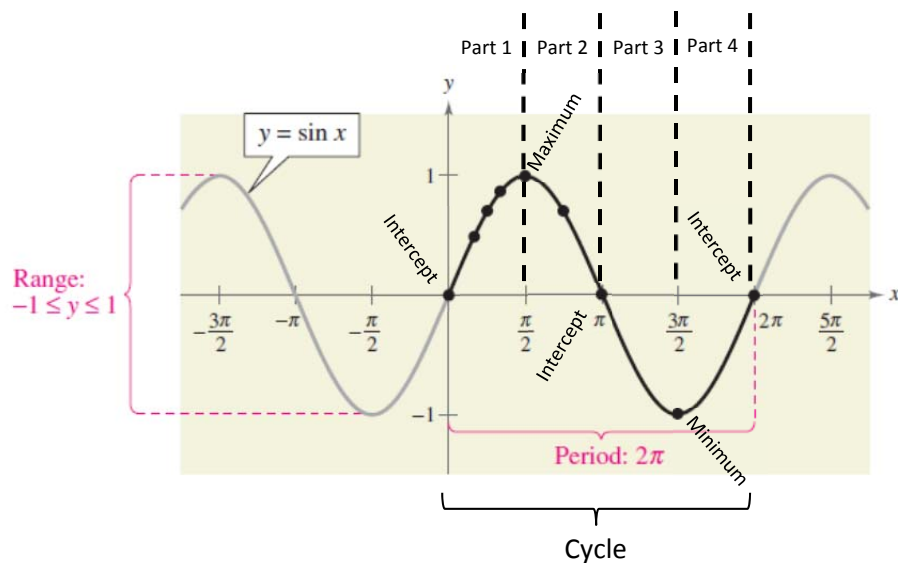


Pg. 321 4.5A – Graphs of Sine and Cosine Functions

The graph of a sine function is an oscillation known as a sine curve.

Parent function of sine: $\sin x$



5 Key Graphing Points

- 1) Intercepts (3 per cycle)
- 2) Maximum (1 per cycle)
- 3) Minimum (1 per cycle)

Note: Cycle is divided into 4 parts.
Normal cycle of sine is 2π .

Thus, each part is $\frac{2\pi}{4}$ or $\frac{\pi}{2}$ units wide.

General equation of sine: $y = a \sin(bx - c) + d$

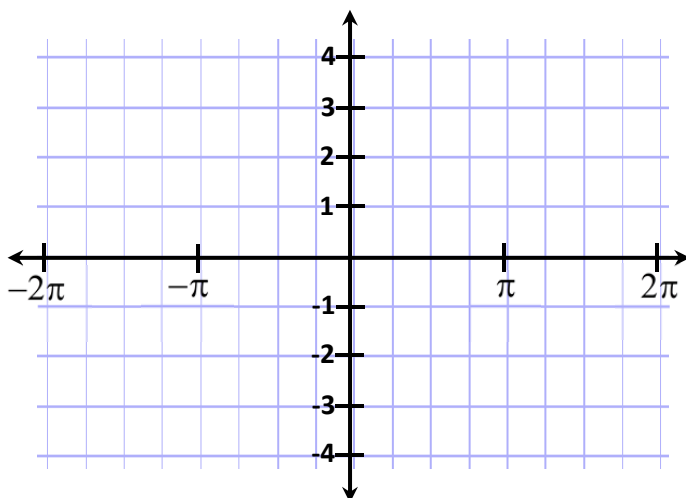
The _____ is half the distance between the maximum and minimum.

Amplitude: $|a|$ **Note:** We take the absolute value because distance is always positive.

If $|a| > 1$, graph is vertically stretched. If $|a| < 1$, then the graph is vertically shrunk.

Ex 1:

Graph $y = 3 \sin x$



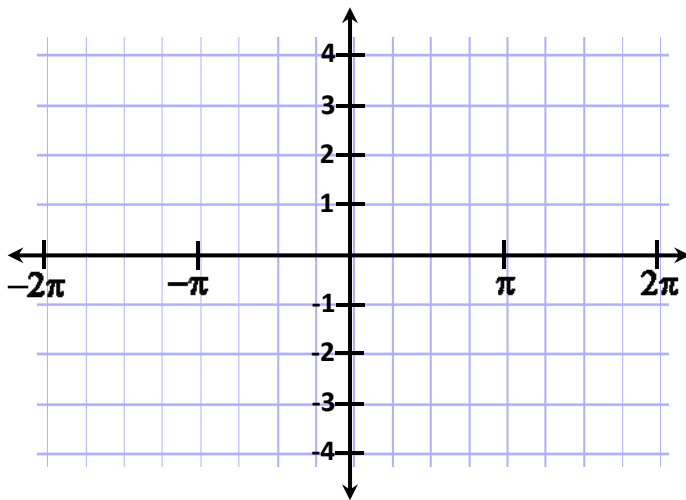
General equation of sine: $y = a \sin(bx - c) + d$

The _____ of a sine function is one complete cycle of the graph.

The normal period for sine is 2π . **Period:** $\frac{\text{Normal Period}}{b} = \frac{2\pi}{b}$

Ex 2:

Graph $y = \sin(2x)$



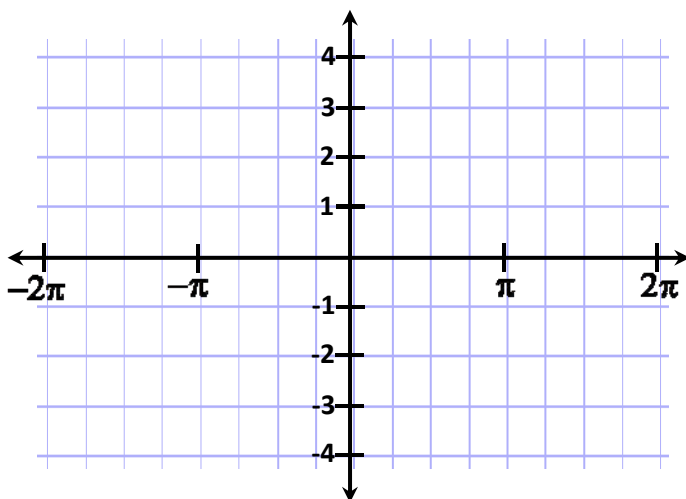
General equation of sine: $y = a \sin(bx - c) + d$

The _____ is the distance the graph is translated horizontally. In other words, the starting point is shifted horizontally.

Phase Shift: **START** Solve for $bx - c = 0$ **FINISH** $x + \text{Period}$

Ex 3:

Graph $y = \sin\left(x - \frac{\pi}{2}\right)$



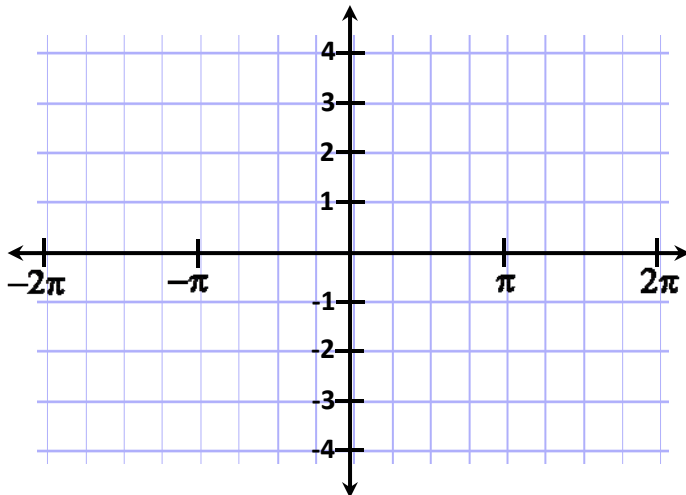
General equation of sine: $y = a \sin(bx - c) + d$

The _____ is the distance the graph is shifted vertically.

Vertical Translation: d

Ex 4:

Graph $y = \sin x + 2$



Bring It All Together:

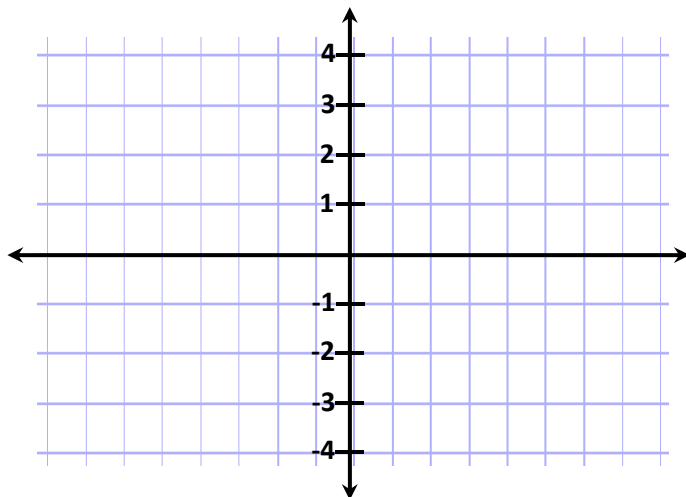
$$y = a \sin(\underbrace{bx - c}_{\text{Phase Shift: } bx - c = 0}) + d$$

Amplitude: $|a|$ Period: $\frac{2\pi}{b}$ Vertical Translation: d

Ex 4:

Graph $y = -3 \sin\left(2x + \frac{\pi}{4}\right) - 1$

Important:
1st Reflect
2nd Shift



Assignment 4.5A Pg. 328 **REQUIRED:** Vocab #'s 1-5

Problem Set #'s 1, 5, 7, 9, 13, 15, 21, 25, 27, 31, 35, 43, 45, 49, 57, 61, 67, 69